Practice Makes Perfect: An Optimization-Based Approach to Controlling Agile Motions for a Quadruped Robot

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An Optimization-based Approach to Controlling Agile Motions for a Quadruped Robot


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Abstract—This work approaches the problem of controlling quadrupedal running and jumping motions with a parametrized, model-based, state-feedback controller. Inspired by the motor learning principles observed in nature, our method automatically fine tunes the parameters of our controller by repeatedly executing slight variations of the same motion task. This learn-through-practice process is performed in simulation in order to best exploit computational resources and to prevent the robot from damaging itself. In order to ensure that the simulation results match the behavior of the hardware platform sufficiently well, we introduce and validate an accurate model of the compliant actuation system. The proposed method is experimentally verified on the torque-controllable quadruped robot StarlETH by executing squat jumps and dynamic gaits such as a running trot, pronk and a bounding gait.

I. INTRODUCTION

Legged locomotion enables humans and animals to traverse difficult environments with agility and grace. Given this remarkable ability, humans and animals have served as a source of inspiration for the field of robotics since its very beginning. However, the locomotion skills of state-of-the-art mobile robots are still very limited compared to those seen in nature. Consequently, the problem of generating motor control behaviors for legged robotic systems remains a very active area of research.

To perform agile motions, especially those that might include airborne phases, a robot needs to be equipped with sufficiently powerful actuators. Fortunately, the development of high-performance drives for legged robots has seen significant progress in recent years. For instance, hydraulic systems such as Boston Dynamic’s quadrupeds [1] (BidDog, AlphaDog and WildCat) as well as IIT’s HyQ [2] feature great performance and enable dynamic gaits such as the flying trot, bound and gallop. Likewise, research on electric actuators contributed to significant improvements in the motor skills of legged robots over the past few years. MIT’s cheetah [3], for instance, uses electric motors with low gear reduction, and is skilled enough to bound over obstacles. Other systems employ biologically inspired actuators which make use of compliant elements, inspired by the fact that humans and animals leverage the elastic nature of their musculoskeletal structures [4]. By exploiting the compliance of the actuation system, the power and velocity output of electric motors can be amplified, as we showed for ScarlETH, a mechanical leg powered by series-elastic actuators [5]. A number of robots, including Marc Raibert’s early machines [6], achieve dynamic maneuvers thanks to the compliance of the system.

As series-elastic actuators (SEA) combine many features essential for legged robots, such as torque control, lightweight design and robustness against impacts, we built a fully articulated quadruped robot, StarlETH [7], with highly compliant SEAs. To increase StarlETH’s repertoire of motion skills, we are interested in developing flexible control strategies for various agile maneuvers including running and jumping. Importantly, one of the main goals of our control strategy is to take full advantage of the actuators’ compliance.

Raibert’s seminal work [6] on monopod hoppers with telescopic legs showed that a simple collection of control rules is applicable to a large set of dynamic motions and robots. Inspired by nature, contact force profiles were manually designed to enable the MIT Cheetah robot [3] to bound over obstacles. Alternatively, optimization algorithms can be used to generate various locomotion tasks by automatically finding appropriate values for parameterized control policies. Such direct policy search methods have been used, for instance, to generate galloping motions in simulation [8], to control muscle activations for simulated bipeds [9], to stabilize a planar bipedal robot [10] and to generate leaping motions for the wheeled quadruped robot PAW [11]. In previous work, we also applied direct policy search methods for motion synthesis. In particular, we employed PI² and ROCK* [12] to generate jumping and hopping maneuvers for our single legged robot, ScarlETH.

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Our work shows that policy search can be successfully applied to complex dynamical systems with high-dimensional state and action space, enabling agile maneuvers. Our work is based on a generic set of motion primitives encoded through cost functions. Inspired by motor learning principles observed in nature, the cost functions are optimized through a trial-and-error process that requires the repeated execution of slight variations of a motion skill. Since executing these practice runs is time consuming and could possibly damage the hardware, our goal is to utilize the policy search method in simulation only. However, to ensure that the optimized control policies work well also on the hardware platform, we must bridge the gap between simulation and the real world. Consequently, an accurate model of the robot is essential. In our previous work [13], we modeled the rigid-body dynamics of the quadruped, but neglected the series-elastic actuators. For highly agile motions such as jumping, the actuator dynamics start to play a very important role and should not be ignored, for two main reasons. First, the behavior predicted by simulation becomes much worse, and the learned model may no longer perform well on the robot. Second, exploiting the dynamics of the actuators is crucial to ensure optimal performance. The key to the success of our method therefore relies on a model of the actuator unit that appropriately trades-off accuracy versus computational complexity.

The control method we describe in this work is designed to be applicable for various types of quadrupedal robots. Nevertheless, we make a few assumptions regarding actuation and perception capabilities in order to generate stable locomotion skills. The block diagram depicted in Fig. 2 gives an overview of our controller, and indicates the sections that describe each building block. Experiments and results are described in section VI, and the paper concludes with a brief discussion in section VII.

II. MECHANICAL MODEL OF THE QUADRUPED

The controller is primarily tailored to the mechanical model as illustrated in Fig. 3. The rigid multi-body system is composed of 13 bodies, which are connected through three actuated revolute joints per leg. This mechanical model is described with the generalized coordinates \( q \in \mathbb{R}^{15} \times SO(3) \), which include the pose of the torso with respect to the world frame and the joint angles. The generalized velocities \( u \in \mathbb{R}^{18} \) are the linear and angular velocities of the torso and the joint velocities.

The quadruped model is a non-smooth scleronomic dynamical system and can be represented by a set of equations of the form

\[
\begin{align*}
M(q) \ddot{q} - h(q, u) - S^\top \tau_j - J^\top \lambda &= 0, \\
\dot{\lambda} &= J_i u \quad \forall i \in I(q).
\end{align*}
\]

The mass matrix in Eq. (1) is denoted by \( M \). The vector \( h \) covers the non-linear terms including Coriolis terms, centripetal terms and impressed generalized forces such as gravitational forces. The joint torques \( \tau_j \) are mapped to the generalized forces with the selection matrix \( S \), whereas the generalized velocities are mapped to the time derivative of the generalized coordinates with matrix \( F(q) \). The interaction between the rigid bodies is described by a set of closed contacts with the contact forces \( \lambda = [\ldots, \lambda_i, \ldots]^\top \) and the generalized force directions \( J_i^\top(q) = [\ldots, J_i^\top(q), \ldots] \), where \( J_i = \frac{\partial \rho_i}{\partial q} \) is the Jacobian of the corresponding contact point \( r_{WP} \). A contact \( i \) between two interacting bodies is said to be active if it is closed on displacement level i.e. it is in \( I(q) := \{i | g_N_i(q) = 0\} \) where \( g_N_i(q) \) describes the displacement of the two bodies in normal direction of a
contact \( i \). Set-valued force laws define the relation between the relative velocity \( \gamma_i(q) \) of a closed contact \( i \) and the corresponding generalized force \( \lambda_i \).

To prohibit a foot from penetrating and pulling on the ground the (closed) contact is modeled as unilateral contact, which can be represented by a normal cone inclusion on velocity level (cf. [14]).

The frictional contact between the feet and the terrain is modeled as Spatial Coulomb friction with a set-valued force law (cf. [14]). The applied force law represents slipping and sticking effects, which are characterized by the single friction parameter \( \mu \).

To include impacts in the equations of motion in Eq. (1), the set-valued force laws have to be supplemented with an impact law. For each normal cone inclusion we use a Newton-type impact law (cf. [14]), and assume a single contact point per foot with an inelastic impact. We note that this hard contact model is a physically accurate approximation of the real foot of StarlETH, which is spherical and only slightly compliant.

To solve the equations of motion with set-valued contact laws in Eq. (1) together with both the impact and impact-free motion, we employ a time-stepping scheme of Moreau (cf. [14]). A large benefit of this simulation method is that the time step between two successive simulation updates can be chosen to be relatively large without the simulation becoming unstable. For the modeled quadruped, the simulation time step can be set equal to the control update step of 2.5 ms. In addition, the simulation results are physically accurate (cf. [14]), which is particularly essential when they are used in optimizations.

### III. Perception

Advanced model-based locomotion controllers rely on fast and accurate feedback of the robot’s state, namely the generalized coordinates \( q \) and velocities \( u \) as well as on information about its environment for motion planning, respectively adaptation.

### IV. Actuation

StarlETH is equipped with series-elastic actuators in all joints as shown in Fig. 1, which enable both accurate joint position and torque tracking using sophisticated feedback control on joint level.

For applications which do not push the actuators to the limits (e.g. [17]), the actuator dynamics can be ignored and the actuators can be considered as perfect torque and position sources. However, this idealization does not hold anymore for highly dynamic maneuvers. In fact, various saturation and frictional effects can lead to a significant divergence of the commanded joint torque or position signals. To design a controller which takes these effects into account and even exploits the dynamics of the actuators (the compliance of the SEAs), a model of the actuation system is required.
Fig. 2 shows a discrete-time model of the drive train of StarEETH, which includes the following components:

1) Velocity controller: The desired motor velocity \( \dot{\varphi}_m^* \) is regulated by a PI-controller with gains \( k_p^* \) and \( k_i^* \) together with an anti-windup, which saturates the state of the integrator at \( s^* \). The loop is updated with time step \( T_m = \frac{1}{f_m} \) and outputs the desired motor current \( I^* \), which is limited to \( I_{max} = 9.4 \text{A} \) on the motor drives.

2) Current controller: A faster PI current controller with time step \( T_m = \frac{1}{f_m} \) gains \( k_d^* \) and \( k_i^* \) and anti-windup saturation \( s^* \) determines the desired motor voltage \( V \).

3) Motor electronics: Motor resistance \( R \) and inductance \( L \) together with the back EMF \( \left( \frac{1}{R_d^*}\dot{\varphi}_m^* \right) \) are part of the motor electronics which define the mapping of the applied voltage \( V \) to the motor current \( I \). The dynamical effects of the power electronics and power supply are neglected. This loop is evaluated at the same rate as the controller to minimize computational load.

4) Motor mechanics: The motor current \( I \) multiplied with the torque constant \( k_t \) yields the motor torque \( \tau_m \), which acts on the motor shaft together with the friction torque \( \tau_f \), and the load at the joint \( \gamma \tau_j \). The equations of motion of the motor shaft defining the motor velocity \( \dot{\varphi}_m \) and position \( \varphi_m \) can be solved with the lumped motor, gearbox and bearing inertia \( \Theta \).

5) Gearbox & joint friction: The friction of the Harmonic drive gearbox can be approximated with a constant \( (c_1) \), linear \( (c_2) \) and cubic \( (c_3) \) term of the motor velocity (cf. [18]). The frictional torque \( \tau_f \) due to radial load \( f_r \), in the bearings is also affecting the dynamics of the actuator.

6) Spring mechanics: The joint torque \( \tau_j \) is a function of the spring deflection \( \delta \), the spring stiffness \( c(\delta) \), the time derivative of the deflection \( \dot{\delta} \), and the damping \( d(\delta) \). For detailed models of the spring characteristics, the interested reader is referred to [5].

Most parameters of the actuator model and the joint controllers are known from datasheets. The remaining parameters are identified based on different experiments (cf. [5]).

The desired motor velocity \( \dot{\varphi}_m^* \) is finally generated by the joint controllers, which regulate either the desired joint torque \( \tau_j^* \) or the desired joint position \( \varphi_j^* \) and velocity \( \dot{\varphi}_j^* \) as described in [5].

V. LOCOMOTION CONTROL

The (deterministic) locomotion control problem for periodic gaits, which minimizes a cost function \( c \), can be stated as:

\[
\begin{align*}
q^*, u^*, \tau_j^*, \lambda^*, \mathcal{I}^*(q^*) &= \text{argmin } c(q, u) \\
\text{s. t. } \phi(t) &= \phi(t + T) \quad \forall t, \quad \{\text{periodicity}\} \\
M(q) \ddot{q} - h(q, u) - S^T \lambda - J^T \lambda &= 0, \quad \{\text{dynamics}\} \\
q_k &= F(q)u, \quad \gamma_i = J_iu \quad \forall i \in \mathcal{I}(q), \quad \{\text{limits}\} \\
q_i &\in \mathcal{Q}, \quad u_i \in \mathcal{U}, \quad \tau_j \in \mathcal{T}, \quad \{\text{limits}\}
\end{align*}
\]

where \( \phi(t) \) is the periodic solution with period-time \( T \). The solution fulfills all dynamic constraints and does not violate any position limits \( \mathcal{Q} \), velocity limits \( \mathcal{U} \) or actuator limits \( \mathcal{T} \). The periodic constraint can be replaced by the constraint \( \phi(T) = \phi^* \) for non-periodic motions like jumps.

In general, this is a hard control problem to solve, because the motion planning/generation problem, which specifies how the legs and the main body should move \( (q^*, u^*) \), and the motion execution/control problem, which determines the desired motion through the desired torques and forces \( (\tau_j^*, \lambda^*) \), are closely coupled by the set of desired contacts \( \mathcal{I}^*(q^*) \). Moreover, robust locomotion is only achieved if the controller is capable of handling large disturbances or unanticipated terrain irregularities or external pushes. As a consequence, motor actions cannot be planned fully offline and tracked in an open-loop fashion, but have to be generated online by a combination of a feedforward and state feedback controller instead.

We employ a model-based controller with a compact, yet flexible parameter space and fine tune these parameters by repeating the same motion task with slight parameter variations until a desired motion is found and all constraints are met. The proposed controller generates a desired motion based on pre-defined motion primitives, which are superimposed by control actions needed for balancing. To find these motion primitives together with other parameters, we reformulate the problem stated in Eq. 2 to

\[
\theta^* = \arg\min_{\theta \in \mathcal{P}} \sum w_k c_k(q, u, \lambda, \varphi_m, \dot{\varphi}_m),
\]

where the optimal parameter set \( \theta^* \) in the admissible set \( \mathcal{P} \) minimizes the weighed sum of the cost terms \( c_k \), which depend on the state trajectory of the robot \( q, u \) and the actuation signals \( \varphi_m, \dot{\varphi}_m \).

A. Motion Parameterization

1) Contact Scheduling: The desired motions of the legs need to be parameterized in space and time. We split the motions into individual motion primitives according to the contact schedule, which defines the set of contacts \( \mathcal{I}^*(q^*) \), and the role of the legs between the contacts. A stance leg supports the main body, whereas a swing leg moves its foot to a new location. A gait pattern can be employed to predetermine the contact schedule. For periodic motions, the gait pattern is defined by 9 parameters, which includes lift-off and landing time for each leg as well as the stride duration \( T \) that defines the period of the cycle. We use a reduced parameterization that can represent both symmetrical and asymmetrical gaits and allows to define the parameters space for a specific type of gait, which helps to optimize the time parameters for a pre-defined gait (cf. [13]).

2) Terrain Adaptation: The motions of the legs need to be (re-)planned according to the encountered terrain. We introduce a control frame \( C \) as illustrated in Fig. 3 to properly define the motions on arbitrary terrain. The z-axis of the control frame \( (e_z^C) \) is aligned with the estimated surface normal and the x-axis \( (e_x^C) \) is parallel to the projected x-axis of the body fixed base frame \( B \) on the ground. The origin of the coordinate system \( C \) is fixed to the origin of
is the height of the hip above the ground and where \( v \) is the high-level velocity command in this control frame, the motion is properly defined and the world frame \( W \) such that only the orientation of the frame is changing over time.

By describing the desired motion (e.g. body orientation) in this control frame, the motion is properly defined and automatically aligned with the terrain. The same holds for high-level velocity commands \( \mathbf{e}^* = [v_x, v_y, \psi]^T \), which are typically given in heading direction \( (v_x e^C_x) \) or lateral direction \( (v_y e^C_y) \) of the robot as well as desired turning rate \( \psi e^C_z \) around the vertical axis.

3) **Motion of Stance Legs:** Since the configurations of all support legs are defined by the fixed foothold locations and the pose of the torso, we define the motions of all support legs through a desired motion of the torso. For balancing, the center of mass is simply kept above the support region. By averaging the position of the legs with weights depending on their role, a smooth motion of the target of the center of mass is planned [19]. The remaining degrees of freedoms like body height above ground and orientation are prescribed by motion primitives. We employ polyharmonic and quintic polynomial splines with periodic constraints to define the feedforward motion of the main body. To reduce kinematic singularities, the default orientation of the torso is adapted to the local inclination of the terrain and superimposed by gait specific motions, like pitching for a bounding gait.

4) **Motion of Swing Legs:** The desired foot point \( F^s \) of a swing leg is defined by the sum of several position vectors as illustrated in Fig. 3. The basic idea is to plan a desired foothold \( F^{td} \) at the end of the swing phase and then interpolate between lift-off position \( F^{lo} \) and this position at touch-down as a function of the swing phase. For ground clearance, a trajectory in \( z \)-direction of the control frame \( C \) is defined using a spline with zero velocity constraints at the begin and end of the swing phase to avoid step inputs to the actuators and minimize impact losses.

The desired foothold location \( F^{td} \) is determined at every control step based on a desired feedforward motion and a superimposed balancing controller. First, a location on the slope \( F^s \) is selected with respect to the hip joint \( H^j \). For locomotion on sloped terrain there are two different strategies: the lever mechanism and the telescopic strut. The lever mechanism projects the hip position along the slope normal, whereas the telescopic strut strategy projects the hip position along the gravity vector. We apply the latter strategy as discussed in [16]. From the selected location on the ground, the desired foothold is defined by the desired traveling distance given by the speed command and the timing given by the gait pattern. In presence of a disturbance, the location of the foothold is corrected by the balancing controller. We employ an adapted version of Raibert’s flight controller [6] for each leg, which predicts the next foothold according to

\[
h^{FB}_p (v^*_r - v_r) \sqrt{\frac{h}{g}},
\]

where \( v^*_r \) is the desired and \( v_r \) the measured reference velocity between associated hip and middle of the torso, \( h \) is the height of the hip above the ground and \( g \) is the gravitational acceleration. The component of the balancing control is weighted by \( r^{FB}_p \) and only active if there is a velocity error.

**B. Motion Execution**

1) **Leg Coordination:** A leg coordinator decides based on the planning given by the gait pattern and contact sensing if a leg is considered to be a support leg and thus is force controlled or if it is a swing leg and position control can be safely used. We further employ an event detector, which identifies for each leg events such as “early” and “late touch-down”, “early” and “late lift-off”, “slipping contact”, “lost contact during stance” and “hitting an obstacle during swing” to trigger different reflex mechanisms.

No special treatments are required for late lift-off and early touch-down. In case of slipping and lost contact during the stance phase the leg is lowered with respect to the ground plane to regain contact as quickly as possible.

2) **Execution of Swing Leg Motion:** The desired swing foot positions are enforced by mapping the Cartesian positions to the desired joint positions \( \phi^*_j \) and velocities \( \dot{\phi}^*_j \) using inverse kinematics, which are subsequently tracked by the joint position controller.

3) **Execution of Torso Motion:** We apply a virtual model controller in combination with a quasi-static force distribution to track the desired motion of the main body while optimally distributing the ground reaction forces. The virtual model controller outputs a desired net force \( \mathbf{f}^* \) and torque \( \mathbf{t}^* \) which should act on the torso to execute the desired motion defined by the desired position \( \mathbf{r}_{WB}^* \), velocity \( \mathbf{v}_B^* \) and acceleration \( \mathbf{a}_B^* \) as well as desired rotation quaternion \( \mathbf{p}_{WB}^* \) and angular velocity \( \omega_{WB}^* \). The controller has the form of

\[
\mathbf{f}^* = \mathbf{K}_p (\mathbf{r}_{WB}^* - \mathbf{r}_{WB}) + \mathbf{K}_d \int (\mathbf{r}_{WB}^* - \mathbf{r}_{WB}) + \mathbf{K}_d (\mathbf{v}_B^* - \mathbf{v}_B) + \mathbf{a}_B^* m - \sum_{k \in B} \mathbf{f}_k^g
\]

\[
\mathbf{t}^* = \mathbf{K}_p (\mathbf{p}_{WB}^* \mathbf{\Theta}_B \mathbf{p}_{WB}) + \mathbf{K}_d \int (\mathbf{p}_{WB}^* \mathbf{\Theta}_B \mathbf{p}_{WB}) + \mathbf{K}_d (\omega_{WB}^* - \omega_{WB}) - \sum_{k \in B} \mathbf{r}_{WS_k} \mathbf{f}_k^g,
\]

where \( \mathbf{f}_k^g \) is the gravitational force acting on body \( k \), \( m \) is the mass of the main body, \( \mathbf{K} \) are the diagonal gain matrices, \( \mathbf{r}_{WS_k} \) is the skew-symmetric matrix defining the cross product of the position vector \( \mathbf{r}_{WS_k} \) from the origin of the world frame to the center of mass of body \( k \), and \( \mathbf{\Theta}_B : \text{SO}(3) \times \text{SO}(3) \rightarrow \mathbb{R}^3, \mathbf{q}_1, \mathbf{q}_2 \rightarrow \log (\mathbf{q}_1 \otimes \mathbf{q}_2^{-1}) \). We note that the integrators are important to compensate for modeling errors, especially for jumping motions where it is important to launch the maneuver from a pre-defined state. All integrator states are limited to account for windup.

The desired net force and net torque need to be generated by the contact forces \( \lambda^* \). To this end, the force distribution computes the desired contact forces for each support leg \( i \) while accounting for the contact constraints \( (\mu, \lambda_{N,i}, \lambda_{T,i}) \) and torque limits \( (\tau_{min,i}, \tau_{max,i}) \) for each joint \( j \). By approximating
the friction cones as pyramids, the problem can be formulated as quadratic program:

\[
\lambda^* = \arg \min_{\lambda} (A\lambda - b)^\top S (A\lambda - b) + \lambda^\top W \lambda
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dynamic gaits can be found in [13].

VI. RESULTS

The presented locomotion controller was implemented on StarlETH and enabled the robot to perform periodic gaits such as static walk, dynamic trot or bound as well as highly dynamic maneuvers like a vertical jump. The robot was fully powered and computation autonomously during all these maneuvers.

A. Periodic Gaits

The sampling-based method successfully tuned 18 control parameters for trotting, bounding and pronking gaits in simulation. Due to reasonably good accordance of the model, the parameters could be directly used on the real platform. Fig. 4 shows the found gait patterns and some snapshots of the real robot performing these gaits. A time series of snapshots is depicted in Fig. 7, which captures two cycles of a pronking gait.

The proposed controller is robust enough to deal with unperceived obstacles up to 10% of the leg length, as well as with external pushes up to 100 N as shown in [7].

Furthermore, the terrain estimation together with the adaptation of the control signals to the modeled ground plane allowed StarlETH to trot on slopes with an angle of up to 21° (38%) as demonstrated in Fig. 6. A 360° turn on the slope verified that the slope estimation works as intended (cf. [16]).

We want to particularly highlight here that we were not able to find control parameters for highly dynamic gaits by hand despite significant effort and extensive experience (and hence intuition) with the machine. However, the optimization approach helped to find a feasible set for more dynamic gaits like a running trot, pronk and bound.

B. High-Dynamic Maneuvers

A sequence of the optimized vertical jump is shown in Fig. 8. The robot’s main body reached the apex height of 0.76 m, which corresponds to 150% of the leg length. The height trajectories of the torso and the left fore foot are depicted in Fig. 5a). The torso height was measured by an external motion capture system (Optitrack), whereas the foot height measurement is based on the state estimation.

To generate this high-dynamic jump whereby the motors encounter several saturation effects, it was particularly important to have an accurate actuator model. As a result, the trajectory, which was optimized in simulation with the actuation model, comes close to the trajectory of the real robot. If the same optimized desired trajectories are applied in simulation without the actuator model, the robot is able to jump much higher than the real robot.

Fig. 5b) shows a good agreement between the measured and predicted gearbox velocities together with the commands from start until take-off of the jump.

The convergence of the optimization is illustrated in Fig. 5c). After 250 iterations with a population of 15 samples, the best-ever seen cost was found.

VII. CONCLUSION

Inspired by the principle of learning through practice, we applied a sampling-based search in order to optimize locomotion controllers that significantly expand the repertoire of motion skills for StarlETH, our quadruped robot. We addressed the high-dimensional, non-smooth nature of the locomotion control problem by finding a good trade-off between feed-forward motion primitives, which are optimized based on the design of the robot, and robust state-feedback control, which compensates modeling errors and sensor noise and rejects unanticipated disturbances. We showed that by appropriately modeling the contact and actuator dynamics of our compliant quadruped, the simulation based optimization results were directly applicable to the real platform. Based on our results, we believe that our approach constitutes an important step towards a fully automatic solution for generating behaviors and motion skills for a wide variety of legged robots. To promote further work in this area, we have open-sourced our implementation of the state estimator and motion controller, both of which can be found on our website: leggedrobotics.ethz.ch.

REFERENCES


1 Video: http://youtu.be/Tj1wreiYrUY
2 Video: http://youtu.be/Wuc7m0hKgO
3 Video: http://youtu.be/NPa9wspVUpg
4 Video: http://youtu.be/aF5xL9NqCmE
Fig. 6. StarlETH transits from flat to sloped terrain with 21° (38%) while trotting (adapted from [16]).

Fig. 7. StarlETH performs a pronking gait while dealing with unperceived obstacles. (adapted from [13]).

Fig. 8. StarlETH performs a vertical jump: start position, take-off, apex height, landing, end position.


